

Simplicity + Symmetry

Some Cosmological Consequences of Conformally Invariant SM and GR

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USC

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Lecture at “Looking for Simplicity” Workshop
Princeton University

- Locally Conformally Invariant Standard Model + Gravity

Collaborators & References:

I.B. + S.H. Chen: 1004.0752; I.B.+ S.H. Chen + N. Turok: 1105.3606

I.B. + S.H. Chen + P. Steinhardt + N. Turok: 1112.2470, 1207.1940

I.B. : 1109.5872, 1209.1068

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 - General formulation of Weyl invariant effective theory and Weyl invariant renormalized theory.

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- 2T-physics behind the scenes

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Simplest theory: Locally Conformal SM+GR, (1307.1848)

- Scaling symmetry (classical) $\left\{ \begin{array}{l} \text{at smallest scales SM is symmetric if quadratic Higgs} = 0 \\ \text{at largest scales, observe} \simeq \text{scale inv. primordial fluctuations} \end{array} \right.$

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- Must avoid massless dilaton, therefore local scale symmetry (Weyl) when coupled to GR

$$\mathcal{L}(x) = \sqrt{-g} \left[\begin{array}{l} \frac{1}{12} (\phi^2 - 2H^\dagger H) R(g) \\ + g^{\mu\nu} \left(\frac{1}{2} \partial_\mu \phi \partial_\nu \phi - D_\mu H^\dagger D_\nu H \right) \\ - \left(\frac{\lambda}{4} (H^\dagger H - \omega^2 \phi^2)^2 + \frac{\lambda'}{4} \phi^4 \right) \\ + L_{\text{SM}} \left(\begin{array}{l} \text{quarks, leptons, gauge bosons, dark matter, } \nu_R \\ \text{Yukawa couplings to H, not to } \phi \text{ except for } \nu_R \end{array} \right) \end{array} \right]$$

conformal scalars: H = electroweak Higgs doublet, ϕ = dilaton, *ghost* — required

$$g_{\mu\nu} \rightarrow \Omega^{-2} g_{\mu\nu}, \quad \phi \rightarrow \Omega \phi, \quad \psi_{q,l} \rightarrow \Omega^{3/2} \psi_{q,l}, \quad A_\mu^{\gamma, W, Z, g} \text{ unchanged}$$

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- No dimensionful constants:** no G_{grav} , no m_{Higgs} , no $m_{q,l,W,Z}$, no Λ_{cosm}

They emerge in **c-gauge**, $\phi(x) \rightarrow \phi_0$, useful at low energy $2H^\dagger H \ll \phi_0^2$

$$\frac{M_{Pl}^2}{2} = \frac{\phi_0^2}{12}, \quad v_{\text{Higgs}}^{246 \text{ GeV}/c^2} = \sqrt{2} \omega \phi_0, \quad \frac{M_{Pl}^2 \Lambda}{2} = \frac{\lambda' \phi_0^4}{4} \text{ same constant source fills entire universe with a scale hierarchy by hand, but stable}$$

Cosmology: can effective grav. const $\frac{1}{12} (\phi_0^2 - 2H^\dagger H)$ change sign (antigravity)? **geodesically complete!**

General theory of Weyl Invariant SM+GR (1307.1848)

- Effective non-renormalizable field th., or Weyl invariant regularization & renormalization

Many scalars: $\left[\frac{1}{12} U(\phi^i) R(g) + g^{\mu\nu} G_{ij}(\phi) \frac{1}{2} \partial_\mu \phi^i \partial_\nu \phi^j - V(\phi^i) \right]$

Weyl.Symm: Homogeneous: $U(t\phi^i) = t^2 U(\phi^i)$, $V(t\phi^i) = t^4 V(\phi^i)$, with

homothety conditions $\partial_j U = -2G_{ij}\phi^j$, $G_{ij}\phi^i\phi^j = -U$. general solutions for U, G, V
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(1008.1540), (1307.1848)
- Only two scalars, H (doublet) and ϕ (no new degree of freedom)

$$\frac{\mathcal{L}(x)}{\sqrt{-g}} = \left[\begin{array}{l} \frac{1}{12} \phi^2 u(z) R(g) - \phi^4 f(z) - G(z) |D_\mu H|^2 \\ + \frac{1}{2} (u(z) - zu'(z) - z^2 G(z)) (\partial_\mu \phi)^2 \\ + \frac{1}{2} \left(\frac{\partial u}{\partial H} + 2G(z) \frac{H^\dagger}{\phi} \right) \partial\phi \cdot DH + h.c. \quad + \dots \\ + L_{SM} \left(\begin{array}{l} \text{quarks, leptons, gauge bosons, darkmatter, } \nu_R \\ \text{Yukawa couplings to H, not to } \phi \text{ except for } \nu_R \end{array} \right) \end{array} \right]$$

$u(z)$, $G(z)$, $f(z)$ general functions of $z = \frac{\sqrt{2}|H|}{\phi}$, [\dots higher derivatives]

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$$\text{Only } \begin{matrix} 2 \\ \text{scalars} \\ H, \phi \end{matrix} \frac{\mathcal{L}(x)}{\sqrt{-g}} = \left[\begin{array}{l} \frac{1}{12} \phi^2 u(z) R(g) - \phi^4 f(z) - G(z) |D_\mu H|^2 \\ + \frac{1}{2} (u(z) - zu'(z) - z^2 G(z)) (\partial_\mu \phi)^2 \\ + \frac{1}{2} \left(\frac{\partial u}{\partial H} + 2G(z) \frac{H^\dagger}{\phi} \right) \partial\phi \cdot DH + h.c. \quad + \dots \\ + L_{SM} \left(\begin{array}{l} \text{quarks, leptons, gauge bosons, darkmatter, } \nu_R \\ \text{Yukawa couplings to H, not to } \phi \text{ except for } \nu_R \end{array} \right) \end{array} \right]$$

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- Field redefinitions: always possible basis for 2 fields with diagonal KE,

$ds^2 = A^2(z) \left(\frac{1}{2} d\phi^2 - dH^\dagger dH \right)$. Two constraints on $u(z)$, $G(z)$, solution:

$G = Z_{ren}(\rightarrow 1)$ and $\phi^2 u(z) = Z_{ren}(\phi^2 - 2H^\dagger H) \Rightarrow$ **Simplest version is**

unique (and geodesically complete!!). Only effect, renormalized potential $\phi^4 f(z)$. 

- Relevant cosmological degrees of freedom (only time dependent homogeneous fields)

$$ds_{\text{Bianchi}_{7,9,10}}^2 = a^2 \left[-d\tau^2 + e^{2(\alpha_1 + \sqrt{3}\alpha_2)} d\sigma_1^2 + e^{2(\alpha_1 - \sqrt{3}\alpha_2)} d\sigma_2^2 + e^{-4\alpha_1} d\sigma_3^2 \right]$$

scale factor $a(\tau)$	anisotropy $\alpha_{1,2}(\tau)$	Higgs $h(\tau)$	dilaton $\phi(\tau)$, $H = \begin{pmatrix} 0 \\ \frac{h(\tau)}{\sqrt{2}} \end{pmatrix}$
radiation density $\frac{\rho_r}{a^4(\tau)}$	fields that couple to Higgs			
	$\frac{\rho_{m_2} h^2(\tau)}{a^2(\tau)}$	$\frac{\rho_{m_1} h(\tau) }{a^3(\tau)}$	scale invariant	

Cosmological Conformal Dynamics (BST), arXiv:1307.1848

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scale invariant				

- Weyl symmetric action: $(a, h, \phi) \rightarrow (\Omega^{-1} a, \Omega h, \Omega \phi)$, **invariants** $ah, a\phi, \frac{h}{\phi}$

$$L = \left\{ \begin{array}{l} \frac{1}{2} (\phi^2 - h^2) a^2 [(\dot{\alpha}_1^2 + \dot{\alpha}_2^2) + \mathcal{K}(\alpha_1, \alpha_2)] - \rho_r \\ -\frac{1}{2} (\partial_\tau(a\phi))^2 + \frac{1}{2} (\partial_\tau(ah))^2 - \rho_{m_1} a |h| - \rho_{m_2} a^2 h^2 \\ -a^4 \left[\frac{\lambda}{4} \left(1 - \varepsilon \ln \frac{h^2}{\omega^2 \phi^2} \right) (h^2 - \omega^2 \phi^2)^2 + \frac{\lambda'}{4} \phi^4 \right] \end{array} \right\} \begin{array}{l} \text{Hamilt}=0 \\ \text{constraint} \\ (G_{00}=T_{00}) \end{array}$$

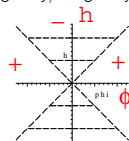
NOTE WEYL INV. RENORMALIZATION
AT SCALE DEFINED BY FIELD

$$\mathcal{K}(\alpha_1, \alpha_2) = \frac{k}{1 - 4\text{sign}(k)} \begin{bmatrix} e^{-8\alpha_1} + 4e^{4\alpha_1} \sinh^2 \left(2\sqrt{3}\alpha_2 \right) \\ -4\text{sign}(k) e^{-2\alpha_1} \cosh \left(2\sqrt{3}\alpha_2 \right) \end{bmatrix} \begin{array}{l} \mathcal{K}=k, \text{ if isotropic, } \alpha_{1,2}=0 \\ \mathcal{K}=0 \text{ if flat } (k=0), \text{ any } \alpha_{1,2} \end{array}$$

Gauges: In gamma-gauge (almost) decoupled dynamics

E-gauge dofs $a_E(\tau), \sigma(\tau)$ for GR interpretation	$\phi_E^2 - h_E^2 = \pm 1 (= \pm 6M_{\text{Pl}}^2),$ $\phi_E^{(\pm)} = \begin{cases} \cosh \sigma \\ \sinh \sigma \end{cases}, h_E^{(\pm)} = \begin{cases} \sinh \sigma \\ \cosh \sigma \end{cases},$ + patch incomplete
c-gauge dofs $a_c(\tau), h_c(\tau) = \text{Higgs}$ for low energy interpretation	$\phi_c(\tau) = \phi_0 = 1$ (using $M_{\text{Pl}} = \frac{1}{\sqrt{6}}$) Geodesically complete, all patches
γ -gauge for computation	$a_\gamma(\tau) = 1$, geodesically complete, all patches degrees of freedom: $\phi_\gamma(\tau), h_\gamma(\tau)$

gravity/antigravity

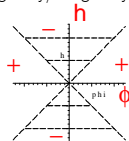


at 45° , $|h/\phi|=1$ invariant
 $a_E=0, h_c = \frac{h}{\phi} \rightarrow \pm 1$

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E-gauge \pm
Ham=0,
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$$\left(\frac{\dot{a}_E}{a_E^2}\right)^2 = \frac{p_1^2 + p_2^2 + p_\sigma^2}{a_E^6} \pm \frac{\rho_r}{a_E^4} \pm \frac{\rho_{m1} |\sinh \sigma|}{a_E^3 |\cosh \sigma|} \pm \frac{\rho_{m2} \frac{\sinh^2 \sigma}{\cosh^2 \sigma}}{a_E^2} - \frac{K(\alpha_1, \alpha_2)}{a_E^2} \pm V(\sigma)$$

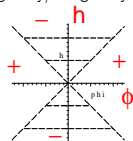
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decoupling $\varepsilon, \omega, p_{1,2} \rightarrow 0$

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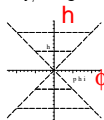
Conversions: obtained by using gauge invariants, $a^2(\phi^2 - h^2)$, $\frac{h}{\phi}$, and $a\phi$

$(E \leftrightarrow \gamma): a_E^2 = |\phi_\gamma^2 - h_\gamma^2|, \left. \begin{matrix} \tanh \sigma \\ \coth \sigma \end{matrix} \right\} = \frac{h_\gamma}{\phi_\gamma} = h_c$ ($\sigma \approx \frac{h_\gamma}{\phi_\gamma}$ when $|h_\gamma| \ll |\phi_\gamma|$)

Gauges: In gamma-gauge (almost) decoupled dynamics

Decoupling limit: neglect anisotropy & $K(\alpha_1, \alpha_2) \rightarrow k$; neglect ε, ω

gravity/antigravity



$|h/\phi|=1$ invariant

$$0 = \left(\begin{aligned} & \cancel{\frac{p_1^2 + p_2^2}{2(\phi_\gamma^2 - h_\gamma^2)}} + \frac{1}{2} K(\alpha_1, \alpha_2) \left(\overset{k}{h_\gamma^2 - \phi_\gamma^2} \right) - \frac{1}{2} p_\phi^2 + \frac{\lambda' \phi_\gamma^4}{4} \\ & + \frac{1}{2} p_h^2 + \rho_r + \rho_{m_1} |h_\gamma| + \rho_{m_2} h_\gamma^2 \\ & + \frac{\lambda}{4} \left(1 - \varepsilon \ln \frac{h_\gamma^2}{\omega^2 \phi_\gamma^2} \right) \left(h_\gamma^2 - \omega^2 \phi_\gamma^2 \right)^2 \end{aligned} \right)$$

Constraint becomes decoupled Hamiltonians $H(h_\gamma) + \rho_r - H(\phi_\gamma) = 0$

$$H(\phi_\gamma) = \frac{1}{2} p_\phi^2 + \frac{1}{2} k \phi_\gamma^2 - \frac{\lambda' \phi_\gamma^4}{4}, \quad H(h_\gamma) = \frac{1}{2} p_h^2 + \rho_{m_1} |h_\gamma| + \rho_{m_2} h_\gamma^2 + \frac{\lambda}{4} h_\gamma^4$$

All solutions: at constant conserved energies $E(\phi_\gamma) = E(h_\gamma) + \rho_r$

Two "particles" each oscillating independently at fixed energies $E(\phi_\gamma)$, $E(h_\gamma)$ in their own potentials with ANY initial conditions. ALL solutions are CYCLIC!!!

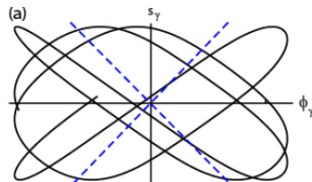
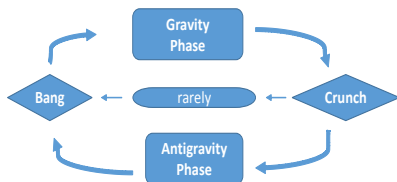
$(\phi_\gamma^2 - h_\gamma^2)$ keeps changing sign!!!! MUST INCLUDE ALL PATCHES!

Analytic (& numerical) solutions, generic behavior

- For special potentials $V(H, \phi)$, obtained **analytically** all cosmological solutions, including **radiation** and **curvature**, with **all initial conditions** (identified 25 regions). This guided numerical analysis of $V_{eff}(H, \phi)$ for the SM, including **anisotropy**.

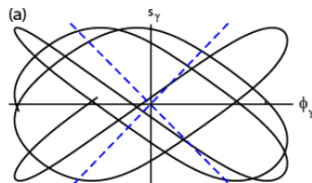
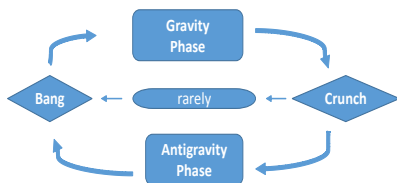
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- All field solutions, ϕ_γ, h_γ (equivalently a_E, σ), α_1, α_2 , continue through singularities. Massless & massive geodesics (information) sail through crunch/bang. Curvature singularities $R_{\mu\nu\lambda\sigma}$ do not stop particle geodesics, even with anisotropy!!.

- Generic **analytic** solution $(\phi_\gamma, h_\gamma, \alpha_{1,2})$ near the singularity is controlled by an attractor driven by [**anisotropy + Higgs kinetic energy + radiation**], all else is subleading (space curvature, inhomogeneities, $V_{eff}(H, \phi)$, cosmological constant)

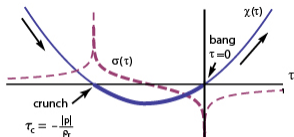
$$\left(\frac{\partial_\tau a_E}{a_E^2}\right)^2 = \frac{\rho_1^2 + \rho_2^2 + \rho_\sigma^2}{a_E^6} \pm \frac{\rho_r}{a_E^4} \pm \frac{\rho_{m1} |\sinh \sigma|}{a_E^3} \pm \frac{\rho_{m2} \sinh^2 \sigma}{a_E^2} - \frac{K(\alpha_1, \alpha_2)}{a_E^2} \pm V(\sigma), \quad \partial_\tau \rho_\sigma = \mp a_E^4 V'(\sigma)$$

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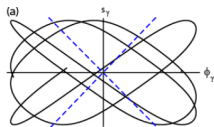
- Singularity resolution: pay attention to conserved quantities, an effective SO(4,2) with 15 conserved charges

Crunch/Antigravity/Bang : $\chi = \phi_\gamma^2 - h_\gamma^2$
 $a_E^2 = |\chi|$



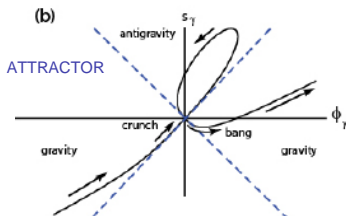
shorter antigravity period with more radiation

antigravity phase *between*
Crunch/Bang, unavoidable,
Resolves classical
cosmological singularities



(a)
 Generic
 cyclic
 gravity/
 antigravity

(b) With anisotropy: both ϕ_γ, h_γ must pass simultaneously through origin, and antigravity



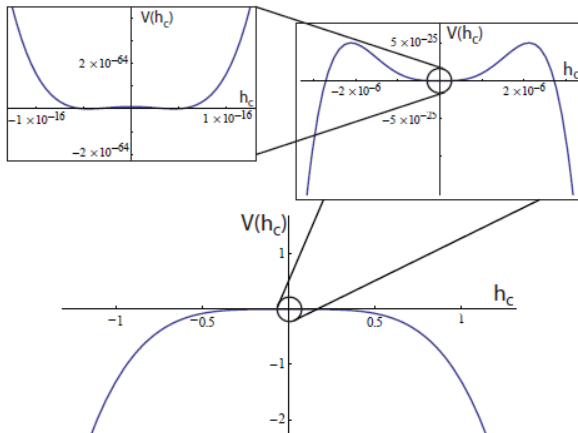
ATTRACTOR

This forces unique initial conditions at each bang !!

Quantum Effective Higgs Potential

A simplified model of $\lambda(h)$ (with the key metastable behavior) in c -gauge ($\omega\phi_0 = v$)

$$V_{\text{eff}}(h) \equiv \lambda_0 \left(1 - \varepsilon \ln \left(\frac{h}{v} \right)^2 \right) (h^2 - v^2)^2, \quad v = 246 \frac{\text{GeV}}{c^2} \simeq \frac{10^{-16}}{4} M_{Pl}$$



Phase Transitions to Planck Scale and Impact on Cosmos

- After phase transition new value of order $h \sim M_{Planck}$.

Huge influence on the the universe through strong interaction with gravity. The universe reacts roughly as if there is a huge negative cosmological constant; bubbles of the new vacuum rapidly fill the universe → **Big Crunch**.

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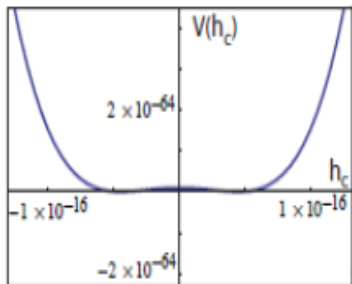
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- New tools were already available: **complete set of analytic cosmological solutions** (BCST).
This is an application of new duality methods in 1T physics generated by 2T-physics.
2T-physics is at the bottom of 1T-physics conformal symmetry $SO(4,2)$, and much more...
(Tell at the end if you ask)

Generic solution in stable vacuum

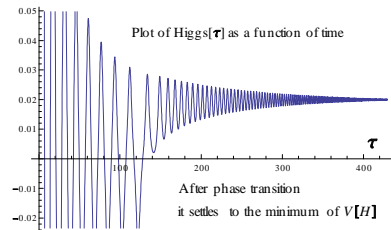
- If stable Higgs vacuum, there is a single cycle (unless there are more scalars, inflaton etc)

If stable vacuum

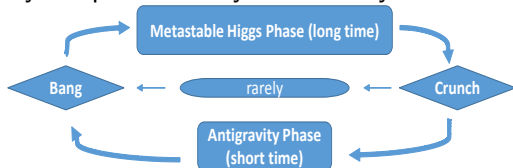


Higgs $h_c = \frac{h_\gamma}{\phi_\gamma} = 1$ emerge **large** at bang

settles to vacuum while universe expands. No cycles.



- Cycles possible only if driven by another scalar field



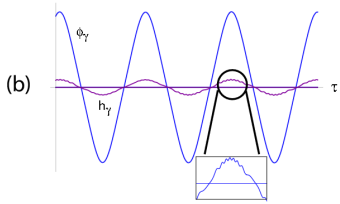
Unstable Vacuum-Narrow band of stable initial conds

The SM Higgs field alone can drive the entire cycle, no additional scalars needed.

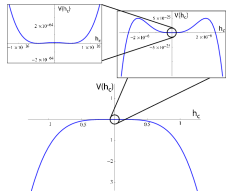
Higgs recaptures metastable state after each Bang

$$\frac{\lambda}{4} \left(1 - \epsilon \ln \frac{h^2}{\omega^2 \phi^2} \right) (h^2 - \omega^2 \phi^2)^2 + \frac{\lambda'}{4} \phi^4$$

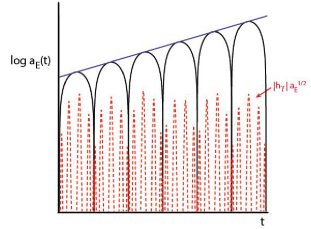
tiny negative λ' imitates tunnelling



Infinite oscillations in effective potential



∞ cycles, entropy produced during antigravity
 ∞ time to $a_E \rightarrow 0$, **no beginning**



Summary and Outlook

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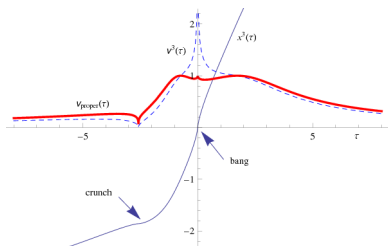
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Geodesically Complete Universe: Info goes through singul.

All geodesics $x^\mu(\lambda)$ in **all SM** cosmologies: $g_{\mu\nu}(x)$, $h(x)$, $m(x) = g_p h(x)$,

$$S_{\text{particle}} = - \int d\lambda \, m(x) \sqrt{-\dot{x}^\mu \dot{x}^\nu g_{\mu\nu}(x)}, \Rightarrow x^i(\tau) = q^i + \int^\tau d\tau' \frac{g_3^{ij}(\tau') k_j}{\sqrt{g_3^{kl}(\tau') k_k k_l + m^2(\tau') a^2(\tau')}}$$

including anisotropy in 3D metric $g_3^{ij}(x(\tau))$



, $m \rightarrow 0$ included

- ▶ $x(\tau)$ for both massive & massless geodesics is finite and continuous throughout
- ▶ The coordinate velocity $v = \dot{x}$ goes to 0 (or ∞) at crunch and ∞ (or 0) at bang.
- ▶ The proper speed $v_{proper} = \sqrt{g_{3ij} \dot{x}^i \dot{x}^j} / \sqrt{g_{3ij} \dot{x}^i \dot{x}^j + m^2 a^2}$, never exceeds unity.
- ▶ Information goes through despite singularity in **all SM** complete geometries

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 - 2 Investigated analytic continuation in complex τ plane. Avoid Planck scale and antigravity region at large contours, so avoid QG. Found complex solution, without cuts in τ , gives the same physically relevant results of geodesically complete classical solutions, by analytic continuation before Crunch and after Bang.

This may be interpreted as semi-classical approximation of the quantum path integral, avoiding singularities

2T-physics and its relation to 1T-physics

For an outline of 2T-physics, mostly in classical mechanics, with a summary of field theoretic formulation, see [arXiv:1004.0688](https://arxiv.org/abs/1004.0688)

Behind BST cosmology there is a deeper theory: 2T SM+GR in 4+2 dims. Concepts and techniques of computation used for analytic results in cosmology originated in studies of 2T gravity and 2T standard model in 4+2 dimensions.

- The Weyl symmetry is a bridge to 4+2 dims, it amounts to coordinate reparametrizations in the extra 1+1 dimensions. [arXiv:0811.2510](https://arxiv.org/abs/0811.2510)
- 2T Physics is an approach with a lot more gauge symmetry, but gauge invariant sector has same physical content as 1T physics (i.e. no exotic stuff) [arXiv:1004.0688](https://arxiv.org/abs/1004.0688)
- 2T physics makes many more predictions in the form of hidden symmetries (e.g. conformal symm) and dualities that 1T-physics cannot predict, but are true
- Duality is the tool used to solve the cosmological equations analytically (amounts to Weyl gauge transformations in the present example)

[more general examples of dualities
in CM or QM: 1311.4205
in Field Theory: 0705.2834](#)